

P425/1
PURE
MATHEMATICS
Paper 1
Nov 2020
3hrs

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Uganda Advanced Certificate of Education
RESOURCEFUL MOCK EXAMINATIONS 2020
PURE MATHEMATICS

Paper 1

3 hours

INSTRUCTIONS TO CANDIDATES:

Attempt **all** the **eight** questions in **Section A** and **Not** more than **five** from **Section B**.

Any additional question(s) will not be marked.

All working must be shown clearly.

Silent non-programmable calculators and mathematical tables with a list of formulae may be used.

Graph papers are provided.

SECTION A: (40MARKS)

Answer **all** the **eight** questions in this Section.

1. Solve the simultaneous equations; $\frac{1}{2y} + \frac{1}{x} = 4$; $\frac{3}{x} - \frac{1}{y} = 7$. (5marks)
2. Prove that; $\frac{\log_2 x - \log_2 x^2}{\log_4 x^3} + \frac{5}{3} = \log 10$. (5marks)
3. Given the parabola $y^2 = 8x$,
 - a) Express a point T on the parabola in parametric form using t as the parameter. (2marks)
 - b) If parameter r gives point R , show that the gradient of chord TR is $\frac{2}{t+r}$. (3marks)
4. Find $\int x^3 e^{x^2} dx$. (5marks)
5. The line $r = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} + \mu \begin{pmatrix} 2 \\ a \\ b \end{pmatrix}$ meets a plane P perpendicularly at the point $(3, 1, 2)$. Find the vector equation of the plane. (5marks)
6. Solve $\sin(120^\circ + 3x) = \cos(90^\circ - x)$ for $0^\circ \leq x \leq 90^\circ$. (5marks)
7. A roll of fencing material $152m$ long is used to enclose a rectangular area using two existing perpendicular walls. Find the maximum area enclosed. (5marks)
8. Solve the differential equation $\frac{dy}{dx}x - x = y$ given that $y = e$ when $x = e$. (5marks)

SECTION B : (60MARKS)

9. a) Prove that; ${}^{n+1}_{r+1}C + {}^{n+1}_{r+2}C = {}^{n+2}_{n-r}C$. (6marks)
b) Two blue, three red and four black beads are to be arranged on a circular ring made of a wire so that the red are separated. Find the number of different arrangements. (6marks)
10. Given that; $f(x) = \frac{1+2x}{1-x}$
 - a) Find Maclaurin's expansion of $f(x)$ upto the term in x^3 . (8marks)
 - b) Hence, find the value of $\frac{1.02}{0.99}$ to four significant figures. (4marks)

11. a) Given that; $y \sin x + x \cos y = \frac{\pi}{2}$, find $\frac{dy}{dx}$. (4marks)

b) A square prism is always three times the width in length. If the volume increases at a constant rate of $4\text{cm}^3\text{s}^{-1}$, find the rate of change of the cross-sectional area when the width is 12cm . (8marks)

12.

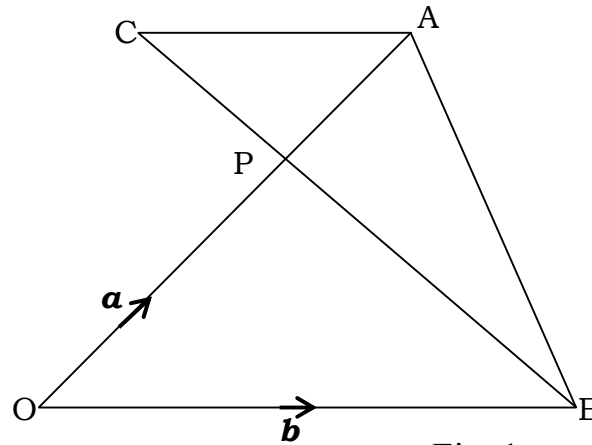


Fig. 1

Figure 1 shows points A and B with position vectors a and b respectively.
 $3AC = BO$.

a) Express each of the following in terms of vectors a and b . (2marks)
 i) BA (3marks)
 ii) BC

b) Find the ratio $BP:PC$ (7marks)

13. a) Prove that $\cos(\tan^{-1}x) = (x^2 + 1)^{-\frac{1}{2}}$. (4marks)

b) i) Prove that $\frac{\cos^2 4x + \cos 4x + \sin^2 4x}{\cos^2 4x - \cos 4x + \sin^2 4x} = 3$ for $0 \leq x \leq \pi$. (4marks)

14. The lines L_1 and L_2 are perpendicular and intersect at $P(0,5)$. Line L_1 meets the x-axis in the first quadrant at Q such that $PQ = 13$ units. If L_2 meets the x-axis at R , without graphical construction, find the area of the triangle PQR . (12marks)

15. Given that $Z_1 = 2 - 3i$, $Z_2 = 1 + 2i$ and $Z_3 = 3 - 4i$.

a) Express $\frac{Z_1 + Z_2}{Z_1 Z_2}$ in the form $a + bi$ where a and b are real numbers. (6marks)
 b) Find a polynomial $p(x)$ of degree four where the roots of $p(x) = 0$ are Z_2 and Z_3 . (6marks)

16. Evaluate; $\int_2^3 \frac{x^4 - x^3 - x^2 + 4x - 1}{(x-1)(x^2+1)} dx$. (12marks)

END